

DISPLAY OF STILL IMAGES THAT
APPEAR ANIMATED TO VIEWERS IN MOTION

Cross Reference to Related Applications

This is a division of United States Patent
5 Application No. 09/888,083, filed June 22, 2001, now U.S.
Patent No. _____, which claims the benefit of United
States Provisional Patent Application No. 60/214,039, filed
June 23, 2000, which is hereby incorporated by reference
herein in its entirety.

10 Background of the Invention

This invention relates to the display of still
images that appear animated to a viewer in motion relative
to those images. More particularly, this invention relates
to the display of still images that can be other than
15 planar and perpendicular to a viewer's line of sight.

Display devices that display still images
appearing to be animated to a viewer in motion are known.
These devices include a series of graduated images (i.e.,
adjacent images that differ slightly and progressively from
20 one to the next). The images are arranged in the direction
of motion of a viewer (e.g., along a railroad) such that
the images are viewed consecutively. As a viewer moves
past these images, they appear animated. The effect is
similar to that of a flip-book. A flip-book has an image
25 on each page that differs slightly from the one before it
and the one after it such that when the pages are flipped,
a viewer perceives animation.

A longstanding trend in mass transportation systems has been the development of installations to provide the passengers in subway systems with animated motion pictures. The animation of these motion pictures is effected by the motion of the viewer relative to the installation, which is fixed to the tunnel walls of the subway system. Such installations have obvious value: the moving picture is viewable through the train windows, through which only darkness would otherwise be visible.

Possible useful moving picture subjects could be selections of artistic value, or informative messages from the transportation system or from an advertiser.

Each of the known arrangements provides for the presentation of a series of graduated images, or "frames," to the viewer/rider so that consecutive frames are viewed one after the other. As is well known, the simple presentation of a series of still images to a moving viewer is perceived as nothing more than a blur if displayed too close to the viewer at a fast rate. Alternatively, at a large distance or low speeds, the viewer sees a series of individual images with no animation. In order to achieve a motion picture effect, known arrangements have introduced methods of displaying each image for extremely short periods of time. With display times of sufficiently short duration, the relative motion between viewer and image is effectively arrested, and blurring is negligible. Methods for arresting the motion have been based on stroboscopic illumination of the images. These methods require precise synchronization between the viewer and the installation in order that each image is illuminated at the same position relative to the viewer, even as the viewer moves at high speed.

The requirements of a stroboscopic device are numerous: the flash must be extremely brief for a fast moving viewer, and therefore correspondingly bright in order that enough light reach the viewer. This

requirement, in turn, requires extremely precisely timed flashes. This precision requires extremely consistent motion on the part of the viewer, with little or no change in speed. All of the aforementioned requirements result in
5 a high level of mechanical or electrical complexity and cost, or greater consistency in train motion than exists. Other known arrangements have overcome the need for high temporal precision by providing a transponder of some sort on the viewer's vehicle and a receiver on the installation
10 to determine the viewer's position. These arrangements involve considerable mechanical and electrical complexity and cost.

The aforementioned known arrangements generally require the viewer to be in a vehicle. This requirement
15 may be imposed because the vehicle carries equipment for timing, lighting, or signaling; or because of the need to maintain high consistency in speed; or to increase the viewer's speed, for example. The use of a vehicle requires a high level of complexity of the design because of the
20 number of mechanical elements and because one frequently is dealing with existing systems, requiring modification of existing equipment. The harsh environment of being mounted on a moving subway car may limit the mechanical or electrical precision attainable in any unit that requires
25 it, or it may require frequent maintenance for a part where high precision has been attained.

The use of a vehicle also imposes constraints. At the most basic level, it limits the range of possible applications to those where viewers are on vehicles. More
30 specifically, considerations of the vehicle's physical dimensions constrain a stroboscopic device's applicability. The design must take into account such information as the vehicle's height and width, its window size and spacing, and the positions of viewers within the vehicle. For
35 example, close spacing of windows on a high speed train requires that stroboscopic discharges preferably be of high

frequency and number in order that the display be visible to all occupants of a train. The dimensions of the environment, such as the physical space available for hardware installation in the subway tunnel and the
5 distances available over which to project images, impose further constraints on the size of elements of any device as well as on the quality and durability of its various parts.

Though in principle a stroboscopic device can
10 work for slowly moving viewers, simply by spacing the projectors more closely, in practice it is difficult. First, closer spacing increases cost and complexity. Also, once the device is installed with a fixed projector-to-projector distance, a minimum speed is imposed on the
15 viewer.

An existing method for the display of animated images involving relative motion between the viewer and the device is the zootrope. The zootrope is a simple hollow cylindrical device that produces animation by way of the
20 geometrical arrangement of slits cut in the cylinder walls and a series of graduated images placed on the inside of the cylinder, one per slit. When the cylinder is spun on its axis, the animation is visible through the (now quickly moving) slits.

The zootrope is, however, fixed in nearly all its proportions because its cross section must be circular. Since the animation requires a minimum frame rate, and the frame rate depends on the rotational speed, only a very short animation can be viewed using a zootrope. Although
25 there is relative motion between the viewer and the apparatus, in practice the viewer cannot comfortably move in a circle around the zootrope. Therefore only one configuration is practicable with a zootrope: that in which a stationary viewer observes a short animation through a
30 rotating cylinder.

For the reasons of its incapacity to be altered in shape, the short duration of its animation, and the fact that it must be spun, the zootrope has remained a toy or curiosity without practical application. However, at least 5 one known system displays images along an outdoor railroad track in an arrangement that might be referred to as a "linear zootrope" in which the images are mounted behind a wall in which slits are provided. That outdoor environment is essentially unconstrained.

10 In view of the foregoing, it would be desirable to provide apparatus for use in a spatially-constrained environment that displays still images that appear animated to a viewer in motion.

15 It would also be desirable to provide such apparatus for use in a spatially-constrained environment in which the side profile of the apparatus can be somewhat conformed to fit better within the spatially-constrained environment.

Summary of the Invention

20 It is an object of this invention to provide apparatus for use in a spatially-constrained environment that displays still images that appear animated to a viewer in motion.

25 It is also an object of this invention to provide such apparatus for use in a spatially-constrained environment in which the side profile of the apparatus can be somewhat conformed to fit better within the spatially-constrained environment.

30 In accordance with this invention, apparatus is provided that displays still images. The still images form an animated display to a viewer moving substantially at a known velocity relative to the images substantially along a known trajectory substantially parallel to the images. The apparatus includes a backboard having a backboard length 35 along the trajectory. The images are mounted on a surface

of the backboard. Each still image has an actual image width and an image center. Image centers are separated by a frame-to-frame distance. A slitboard is positioned substantially parallel to the backboard facing the surface
5 upon which the images are mounted and is separated therefrom by a board-to-board distance. The slitboard is mounted at a viewing distance from the trajectory. The board-to-board distance and the viewing distance total a backboard distance. The slitboard has a slitboard length
10 along the trajectory and has a plurality of slits substantially perpendicular to the slitboard length. Each slit corresponds to a respective image and has a slit width measured along the slitboard length and a slit center. Respective slit centers of adjacent slits are preferably
15 separated by the frame-to-frame distance.

The side profiles of the slitboard and backboard (viewable either cross-sectionally or elevationally in the same direction as the trajectory) can be preferably as follows:

- 20 1) parallel to each other, planar, and perpendicular (e.g., vertical) to a viewer's (e.g., horizontal) line of sight;
- 2) parallel to each other, planar, and non-perpendicular (e.g., slanted) to a viewer's line of
25 sight;
- 3) parallel to each other, nonplanar (e.g., curved), and non-perpendicular to a viewer's line of sight; and
- 4) nonparallel, nonplanar, and non-perpendicular.

30 This advantageously allows the apparatus to be constructed such that its side profile can be conformed to fit better within a spatially-constrained environment, such as, for example, a subway tunnel.

Brief Description of the Drawings

The above and other objects and advantages of the invention will be apparent upon consideration of the following detailed description, taken in conjunction with 5 the accompanying drawings, in which like reference characters refer to like parts throughout, and in which:

FIG. 1 is a perspective view of an illustrative embodiment of apparatus according to the invention;

10 FIG. 2 is an exploded perspective view of the apparatus of FIG. 1;

FIG. 2A is a perspective view of an alternative illustrative embodiment of the apparatus of FIGS. 1 and 2;

15 FIG. 3 is a schematic plan view diagram of the geometry and optics of the apparatus of FIGS. 1 and 2;

FIG. 3A is a schematic plan view diagram of the 20 geometry of a curved embodiment of the invention;

FIGS. 4A, 4B and 4C (collectively "FIG. 4") are schematic plan view representations of a single image and slit with a viewer at three different positions at three

different instants of time;

FIGS. 5A, 5B and 5C (collectively "FIG. 5") are schematic plan view representations of a pair of images and slits with a viewer at three different positions at three different instants of time;

25 FIG. 6 is a schematic plan view representation of a single image being viewed by a viewer over time, illustrating the stretching effect;

FIG. 6A is a schematic plan view representation 30 illustrating the stretching effect where the backboard is not parallel to the direction of motion;

FIG. 7 is a schematic plan view of a second 35 illustrative embodiment of the invention wherein the images are curved;

FIG. 8 is a schematic plan view of a third illustrative embodiment of the invention wherein the images are inclined relative to the backboard;

5 FIG. 9 is a schematic plan view of a fourth illustrative embodiment of the invention, similar to the embodiment of FIG. 8, but wherein the slitboard includes a series of sections parallel to the images and inclined relative to the backboard;

10 FIG. 10 is a schematic perspective representation of a pair of combination slitboard/backboards from a fifth illustrative embodiment of the invention which is two-sided;

15 FIG. 11 is a schematic plan view of the embodiment of FIG. 10;

FIG. 12 is a schematic plan view of a sixth embodiment having curved images such as in the embodiment of FIG. 7, and being two-sided such as in the embodiment of FIGS. 10 and 11;

20 FIG. 13 is a perspective view of a roller-type image holder for use in a seventh illustrative embodiment of the invention;

FIG. 14 is a perspective view of an eighth illustrative embodiment of the invention;

25 FIG. 15 is a vertical cross-sectional view, taken from line 15-15 of FIG. 14, of the eighth illustrative embodiment of the invention;

FIG. 16 is a simplified perspective view showing the mounting of a plurality of modular units in a subway tunnel according to the invention;

30 FIG. 17 is a schematic side view representation of an embodiment of the invention showing the profiles of the slitboard and backboard;

35 FIG. 18 is a schematic cross-sectional view of a subway tunnel showing the embodiment of the invention shown in FIG. 17 mounted therein;

FIG. 19 is a schematic cross-sectional view of a subway tunnel showing another embodiment of the invention mounted therein;

FIGS. 20 and 21 are schematic side view representations of the embodiment of the invention shown in FIG. 19 showing the profiles of the slitboard and backboard;

FIG. 22 is a schematic cross-sectional view of a subway tunnel showing still another embodiment of the invention mounted therein;

FIG. 23 is a schematic side view representation of yet another embodiment of the invention showing the profiles of the slitboard and backboard;

FIG. 24 is a schematic side view representation of a further embodiment of the invention showing the profiles of the slitboard and backboard; and

FIG. 25 is a flow diagram of a process for determining whether selected profiles for the slitboard and backboard result in acceptable animation according to the invention.

Detailed Description of the Invention

The present invention preferably produces simple apparatus operating on principles of simple geometric optics that displays animation to a viewer in motion relative to it. The apparatus requires substantially only that the viewer move in a substantially predictable path at a substantially predictable speed. There are many common instances that meet this criterion, including, but not limited to, riders on subway trains, pedestrian on walkways or sidewalks, passengers on surface trains, passengers in motor vehicles, passengers in elevators, and so on. For the remainder of this document, for ease of description, reference will primarily be made to a particular exemplary application -- an installation in a subway system, viewable

by riders on a subway train -- but the present invention is not limited to such an application.

Benefits of the present invention include the following:

- 5 1. A viewer preferably does not need to be in a vehicle.
- 10 2. Complex stroboscopic illumination is preferably not needed.
- 15 3. Precise timing or positioning triggers between the apparatus and the viewer are preferably not needed.
- 20 4. Moving parts are preferably not needed.
- 25 5. Preferably, no shutter is required.
- 30 6. Preferably, no special equipment mounted on the viewer or the viewer's vehicle, if the viewer is in a vehicle, is required.
7. Preferably, no transfer of information between the apparatus and the viewer pertaining to the viewer's position, speed, or direction of motion is needed.
8. A very high depth of field of viewability is preferably offered.
9. Operation independent of the direction of a viewer's motion can be designed.
10. It preferably is effective for each member of a closely spaced series of viewers, independent of their spacing or relative motions.
11. Optics no more precise than a simple slit is preferably required (although other optics may be used).
12. No correlation between vehicle window spacing and picture spacing is preferably required.

13. It preferably offers the possibility of effective magnification of the image in the direction of motion.
- 5 14. Very low minimum viewer speed is preferably required because the magnification allows very close spacing of graduated images.
15. No particular geometry, be it circular, linear, or any other geometry is preferably required.
- 10 16. It preferably has no maximum speed.

The apparatus preferably includes a series of graduated pictures ("images" or "frames") spaced at preferably regular intervals and, preferably between the pictures and the viewer, an optical arrangement that preferably restricts the viewer's view to a thin strip of each picture. This optical arrangement preferably is an opaque material with a series of thin, transparent slits in it, oriented with the long dimension of the slit perpendicular to the direction of the viewer's motion. The series of pictures will generally be called a "backboard" and the preferred optical arrangement will generally be called a "slitboard."

Not essential to the invention, but often desirable, is a source of illumination so that the pictures are brighter than the viewer's environment. The illumination can back-light the pictures or can be placed between the slitboard and backboard to front-light the pictures substantially without illuminating the viewer's environment. When lighting is used it preferably should be constant in brightness. Natural or ambient light can be used. If ambient light is sufficient, the apparatus can be operated without any built-in source of illumination.

Also not necessary, but often desirable, is to make the viewer side of the slitboard dark or nonreflecting, or both, in order to maximize the contrast between the pictures viewable through the slitboard and the

slitboard itself. However, the slitboard need not necessarily be dark or nonreflective. For example, the viewer face of the slitboard could have a conventional billboard placed on it with slits cut at the desired 5 positions. This configuration is particularly useful in places where some viewers are moving relative to the device and others are stationary. This may occur, for example, at a subway station where an express train passes through without stopping, but passengers waiting for a local train 10 stand on the platform. The moving viewers preferably will see the animation through the imperceptible blur of the conventional billboard on the slitboard front. The stationary viewers preferably will see only the conventional billboard.

15 The invention will now be described with reference to FIGS. 1-16.

The basic construction of a preferred embodiment of a display apparatus 10 according to the invention is shown in FIGS. 1 and 2. In this embodiment, apparatus 10 20 is essentially a rectangular solid formed by housing 20 and lid 21. The front and rear of apparatus 10 preferably are formed by slitboard 22 and backboard 23, which are described in more detail below. Slitboard 22 and backboard 23 preferably fit into slots 24 in housing 20 25 which are provided for that purpose. Lightframe 25 preferably is interposed between housing 20 and lid 21 and preferably encloses light source 26, which preferably includes two fluorescent tubes 27, to light images, or "frames" 230, on backboard 23. Slitboard 22 preferably 30 includes a plurality of slits 220 as described in more detail below. Preferably, in order to keep foreign matter out of apparatus 10, particularly if it is to be used in a harsh or dirty environment such as a subway tunnel, each slit 220 is covered by a light-transmissive, preferably 35 transparent cover 221 (only one shown). Alternatively, each slit 220 may be covered by a semicylindrical lens 222

(only one shown), which also improves the resolution of viewed images. Specifically, if the focal length of the lens is approximately equal to the distance between slitboard 22 and backboard 23, the resolution of the image 5 may be increased. This improvement of the resolution is effected by narrowing the width of the sliver of the actual image visible at a given instant by the viewer. Alternatively, the use of lenses may allow the slit width to be increased without lowering resolution.

10 In an alternative embodiment 200, shown in FIG. 2A, housing 201 is similar to housing 20, except that it includes light-transmissive, preferably transparent, front and rear walls 202, 203 respectively, forming a completely enclosed structure. At least one of walls 202, 15 203 (as shown, it is wall 202) preferably is hinged as at 204 to form a maintenance door 205 which may be opened, e.g., to replace backboard 23 (to change the images 230 thereon) or to change light bulbs 27). As shown in FIG. 2A, light bulbs 27 are provided in a backlight 20 20 instead of lightframe 25, necessitating that backboard 23 and images 230 be light-transmissive. Of course, embodiment 200 could be used with lightframe 25 instead of backlight unit 206. Similarly, apparatus 10 could be provided with backlight unit 206 instead of 25 lightframe 25, in which case backboard 23 and images 230 would be light-transmissive.

FIG. 3 is a schematic plan view of a portion of apparatus 10 being observed by a viewer 30 moving at a substantially constant velocity V_w along a track 31 30 substantially parallel to apparatus 10. Track 31 is drawn as a schematic representation of a railroad track, but may be any known trajectory such as a highway, or a walkway or sidewalk, on which viewers move substantially at a known substantially constant velocity.

35 The following variables may be defined from FIG. 3:

D_s = slit width

D_{ff} = frame-to-frame distance

D_{bs} = backboard-to-slitboard distance

V_w = speed of viewer relative to apparatus

5 D_{sb} = thickness of slitboard

D_i = actual width of a single image frame

D_{vs} = distance from viewer to slitboard

Other parameters, which are not labeled, will be
described below, including B (brightness), c (contrast),
10 and D_i' (apparent or perceived width of a single image
frame).

An alternative geometry is shown in FIG. 3A,
where track 31' is curved, and slitboard 22' and
backboard 23' are correspondingly curved, so that all three
15 are substantially "parallel" to one another. Although not
labeled in FIG. 3A, the other parameters are the same as in
FIG. 3, except that, depending on the degree of curvature,
there may be some adjustment in the amount of stretching or
enlargement of the image as discussed below.

20 One of the most significant departures of the
present invention from previously known apparatus designed
to be viewed from a moving vehicle is that no attempt is
made to arrest the apparent motion of the image. That is,
in the present device the image is always in motion
25 relative to the viewer, and some part of the image is
always viewable by the viewer. This contrasts with known
systems for moving viewers where a stroboscopic flash is
designed to be as close as instantaneous as possible in
order to achieve an apparent cessation of motion of an
30 individual image frame, despite its true motion relative to
the viewer.

As with all animation, the apparatus according to
the invention relies on the well known effect of
35 persistence of vision, whereby a viewer perceives a
continuous moving image when shown a series of discrete
images. The operation of the invention uses two distinct,

but simultaneous, manifestations of persistence of vision. The first occurs in the eye reconstructing a full coherent image, apparently entirely visible at once, when actually shown a small sliver of the image that sweeps over the 5 whole image. The second is the usual effect of the flip-book, whereby a series of graduated images is perceived to be a continuous animation.

FIG. 4 illustrates the first persistence of vision effect. It shows the position of viewer 30 relative 10 to one image at successive points (FIGS. 4A, 4B, 4C) in time. In each of FIGS. 4A, 4B and 4C, double-ended arrow 40 represents the total actual image width, D_1 , while distance 41 represents the portion of the image visible at a given time. This diagram shows that viewer 30, over a 15 short period of time, gets to see each part of the image. However, at any given instant only a thin sliver of the picture, of width 41, is visible. Because the period of time over which the sliver is visible is very short, and therefore the motion of the image viewed through the slit 20 in that time is very small, the viewer perceives very little or no blur, even at very high speeds. There is no theoretical upper limit on the speed at which the apparatus works -- the faster the viewer moves, the less time a given sliver is visible. That is, the effect that would cause 25 blur -- the viewer's increased speed -- is canceled by effect that reduces blur -- the period of viewability of a given sliver.

In FIG. 4 the representation of movement of the viewer's eye is purely illustrative. In practice the 30 viewer's gaze is fixed at a screen that is perceived to be stationary, and the entirety of the frame can be seen through peripheral vision, as with a conventional billboard.

FIG. 5 illustrates the second persistence of vision effect. It shows viewer 30 looking in a fixed 35 direction at three successive points in time. In FIG. 5A,

a thin sliver of a first image n is in the direct line of the viewer's gaze through slit 221. In FIG. 5B, the viewer's direct gaze falls on a blocking part of slitboard 22. For the duration that the opaque part of 5 slitboard 22 is in the line of the viewer's direct gaze, the viewer continues to perceive the sliver of image n just seen through slit 221. In FIG. 5C, the direct line of the viewer's gaze falls on slit 222, adjacent to slit 221, and viewer 30 sees a sliver of adjacent image n+1. Because 10 each slit 221, 222 preferably is substantially perfectly aligned with its respective image, the slivers visible at a given angle in the two separate slots preferably correspond substantially precisely. That is, at a position, say, three inches from the left edge of the picture, the sliver 15 three inches from the left edge of the picture is viewable from one frame to the next, and never a sliver from any other part of the image. In this way, the alignment between the slit and the image prevents the confusion and blur perceived by the viewer that otherwise would be caused 20 by the fast motion of the images. Because successive frames differ slightly as with successive images in conventional animations, the viewer perceives animation.

The two persistence of vision effects operate simultaneously in practice. Above a minimum threshold 25 speed, viewer 30 perceives neither discrete images nor discrete slivers.

A very useful effect of apparatus 10 is the apparent stretching, or widening, of the image in the direction of motion. FIG. 6 illustrates the geometrical 30 considerations explaining this stretching effect. Labeled "Position 1" and "Position 2" are the two positions of a given frame 230 where the opposite edges of frame 230 are visible. Because the positions of frame 230 and slit 220 are fixed relative to each other, they precisely determine 35 the angle at which viewer 30 must look in order that slit 220 be aligned with an edge of the image 230.

At Position 1, the left edge of image 230 is aligned with slit 220 and the viewer's eye. At Position 2, the right edge of image 230 is aligned with slit 220 and the viewer's eye. In fact, the two positions occur at 5 different times, but, as explained above, this is not observed by the viewer 30. Only one full image is observed.

If x is the distance from the centerpoint between the two positions of slit 220 to either of the individual 10 positions at Position 1 or Position 2, then the perceived width of the image, D_i' , is $2x$. By similar triangles,

$$D_{vs}/x = (D_{vs} + D_{bs}) / (x + D_i/2)$$

$$x(D_{vs} + D_{bs}) = (x + D_i/2)D_{vs}$$

$$2x = (D_{vs}/D_{bs})D_i$$

$$15 \quad D_i' = (D_{vs}/D_{bs})D_i \quad (1)$$

Thus the perceived width of the image, D_i' , is increased over the actual width of the image by a factor of the ratio of the viewer-slitboard distance to the slitboard-backboard distance.

20 FIG. 6A shows the magnification effect when the backboard 23' is not substantially parallel to the viewer's trajectory. The magnification is found by defining a formula $f(x)$, where x is the distance along the viewer's trajectory, for the shape of the backboard -- that is, the 25 distance of the backboard from the axis defined by the viewer's trajectory -- around each slit (for example, FIG. 7 shows a backboard 71 on which each image 730 forms a semicircle around its respective slit 220). For ease of convention, one can define an x axis along the direction of 30 the viewer's motion and a y axis perpendicular to the x axis and choose the origin at the position of the viewer 30.

To find the magnification, one determines how an arbitrary picture element 230' on the backboard 23' will 35 appear to viewer 30 on a projected flat backboard 23". In FIG. 6A, a section of the true backboard 23' is shown

between slitboard 22 and the projected backboard 23". A length PR of the backboard 23' defines a picture element 230'. This section 230' will appear to viewer 30 as if on projected flat backboard 23", as indicated.

5 For ease of presentation, the section of backboard 23' shown is a straight line segment, but this linearity is not required. Also, the backboard shape does not need to be perfectly described by a formula $y=f(x)$. In practice one can approximate the backboard's true shape in
10 a number of ways -- for example, by treating the backboard as a series of infinitesimal elements, each of which can be approximated by a line segment.

Viewer 30, at position A, sees the left edge P of picture element 230' when slit 220 is at Q. Because the
15 positions of picture element 230' and slit 220 are fixed relative to each other, they precisely determine the angle at which viewer 30 must look in order that slit 220 be aligned with an edge of the element 230'. Therefore, the right edge R of this picture element 230' will be visible
20 when the device has moved relative to viewer 30 to a position where a line parallel to QR passes through A.

The left edge of picture element 230' will appear on projected backboard 23" at position B, a distance Δx from the y axis. The right edge of picture element 230'
25 will appear on projected backboard 23" at position C. The apparent width of the image, D_1' , is the distance BC.

Point P is the intersection of backboard 23' with the line through A and B.

Point Q is the intersection of slitboard 22 with
30 the line through A and B.

Point R is the intersection of backboard 23' with the line through Q and R.

The distance D_1 is the distance from P to R.

35 The coordinates of the point P, (P_x, P_y) , are the solution (x, y) to $y=f(x)$ and

$$y = (D_{vb}/\Delta x)x, \quad (A)$$

where the latter equation is the formula for the line through A and B.

The coordinates of point Q, (Q_x, Q_y), are the solution (x, y) to $y = (D_{vb}/\Delta x)x$, and

5 $y = D_{bs} . \quad (B)$

The coordinates of point R, (R_x, R_y), are the solution (x, y) to $y = f(x)$ and

$$y - Q_y = ((\Delta x + D_i') / D_{vb}) (x - Q_x) . \quad (C)$$

Finally, the size D_i that picture element 230' 10 should have in order that it stretch to size D_i' is given by

$$D_i = ((R_x - P_x)^2 + (R_y - P_y)^2)^{0.5} , \quad (D)$$

where the variables on the right hand side can all be found in terms of dimensions of the apparatus and Δx .

15 The above derivations demonstrate practical methods for determining the stretching effect in order to preshrink an image for either substantially parallel or nonparallel backboards. A useful rule of thumb which is true for either backboard configuration comes from the fact 20 that angle BAC is equal to angle BQR -- the angular size of the projected image as seen by the viewer is the same as the angular size of the actual image at the position of slit 220.

In order to preshrink an image, it can be divided 25 into many elements, starting at $\Delta x=0$ and moving sequentially in either direction while incrementing Δx appropriately. Then each element can be preshrunk and placed at the appropriate location on the backboard.

30 In cases where the viewer's trajectory is curved, such as the geometry shown in FIG. 3A, neither the slitboard nor the backboard will necessarily be a straight line. A similar derivation can be used to the one for nonparallel backboards, by defining a function $g(x)$ for the path of the slit relative to the viewer and replacing 35 Relation (B) with $y=g(x)$.

In practice, the images may be shrunk in the direction of motion before being mounted on the backboard in order that when projected they are stretched to their proper proportions, allowing a large image to be presented
5 in a relatively smaller space. Curved or inclined surfaces on the backboard can be used to augment the effect. That is, as a nonplanar backboard approaches the slitboard, the magnification increases greatly. However, for simplicity, the discussion that follows will assume a planar backboard
10 unless otherwise indicated.

As shown below, the stretching effect, when adjusted through the relevant variable parameters of apparatus 10, can be very useful. Also, the relation between the perceived image size, D_i' , and the viewer
15 distance, D_{vs} , is linear -- the image gets bigger as the viewer moves farther away. This can be a useful effect in the right environment.

There are some limitations and side effects. Both effects of persistence of vision require minimum
20 speeds that are not necessarily equal. Too slow a speed can result in the appearance of only discrete vertical lines, or flicker, or a lack of observed animation effect. In practice, the appearance of only discrete vertical lines is the dominant limitation. A possibly useful effect of
25 the stretching effect arises from the fact that slivers of multiple frames are visible at the same time. That is, if the perceived image is ten times larger than the true image, slivers of ten different images may be visible at any given time. Because each frame presents a different
30 point in time in the animation, multiple times of the image may be simultaneously viewable. This effect may, for example, be used to interlace images, if desired. Similarly, multiple instances of a single frame can be displayed, in a manner similar to that used in commercial
35 motion picture projection. Alternatively, the effect can also result in confusion or blur perceived by viewer 30.

In practice this confusion is barely noticeable, however, and can be reduced through a higher frame rate or a slower varying subject of animation.

Another possibly useful effect occurs when the
5 image of one frame 230 is visible through the slit 220 corresponding to an adjacent frame 230. In this case, multiple side-by-side animations may be visible to the viewer. These "second-order" images can be used for graphic effect, if desired. Or, if not desired, they may
10 be removed by increasing slitboard thickness D_{sb} or the ratio D_{ff}/D_i , by introducing a light baffle 32 between slitboard 22 and backboard 23, or by altering the geometry of backboard 23. All of these techniques are described below.

15 Still another possibly useful effect arises from the fact that the stretching effect distorts the proportions of image 230. One can remove this effect, if not desired, by preshrinking the images 230 so that the stretching effect restores the true proportions. Care must
20 be taken, however, in the case where different viewers 30 observe apparatus 10, each from a different D_{vs} . In this case, the exact restoration to perfect dimensions occurs at one D_{vs} only. At another D_{vs} , the restoration is not exact. In practice, however, for many useful ranges of parameters,
25 the improper proportions have few or no adverse effects.

In general, four parameters are imposed by the environment -- V_w , D_{bs} , D_{vs} , and D_i' . V_w , the viewer's speed, is generally imposed by, e.g., the speed of the vehicle, typical viewer footspeed, or the speed of a moving
30 walkway, escalator, etc. D_{bs} , the backboard-to-slitboard distance, is generally limited by the space between a train and the tunnel wall, or the available space of a pedestrian walkway, for example. D_{vs} , the distance from viewer to slitboard, is imposed by, for example, the width of a
35 subway car or the width of a pedestrian walkway. Finally, D_i' , the perceived image width, should be no larger than

the area visible to viewer 30 at a given instant -- for example, the width of a train window.

Also generally imposed is the well-established minimum frame rate for the successful perception of the animation effect -- viz., approximately 15-20 frames per second. The frame rate, the frame-to-frame distance, and viewer speed are related by

$$\text{Frame rate} = V_w/D_{ff} \quad (2)$$

Because the frame rate must generally be greater than the minimum threshold, and V_w is generally imposed by the environment, this relation sets a maximum D_{ff} .

For example, for a train moving at about 30 miles per hour (about 48 kilometers per hour), given a minimum frame rate of about 20 frames per second, the relation above determines that D_{ff} can be as great as about 2 feet (about 67 cm).

Alternatively, the minimum V_w is determined by the minimum D_{ff} allowable by the image, which is constrained by the fact that D_{ff} can be no smaller than D_i . The stretching effect theoretically allows D_i to be lowered arbitrarily without lowering D_i' , because D_{bs} can, in principle, be lowered arbitrarily. In practice, however, D_{bs} cannot be lowered arbitrarily, because very small values result in very different perceived image widths for each viewer 30 at a different D_{vs} . That is, at too small a D_{bs} , viewers on opposite sides of a train could see too markedly differently proportioned images. Moreover, small D_{bs} , resulting in high magnification, requires correspondingly high image quality or printing resolution.

If viewers at different distances D_{vs} will observe apparatus 10, the closest ones (those with the smallest D_{vs}) generally determine the limits on D_{bs} .

Because images cannot overlap,

$$D_i \leq D_{ff}. \quad (3)$$

If $D_i = D_{ff}$ and one can view second order images, they will appear to abut the first order image, slightly out of

synchronization. The resulting appearance will be like that of multiple television sets next to each other and starting their programs at slightly different times. This effect may be used for graphic intent, or, if not desired, 5 three variations in parameters can remove it.

First, one can decrease the ratio D_i/D_{ff} , effectively putting space between adjacent images. This change will send second order images away from the primary ones.

10 Second, one may increase slitboard thickness D_{sb} so that second order images are obscured by the cutoff angle. That is, for any non-zero thickness of slitboard 22, there will be an angle through which if one looks one will not be able to see through the slits. As 15 the thickness of slitboard 22 increases, this angle gets smaller, and can be seen to follow the relation

$$D_{sb}/D_s \leq D_{bs}/(D_i/2) \quad (4)$$

This relation may alternatively be written

$$D_{sb}/D_s \leq D_{vs}/(D_i'/2) \quad (5)$$

20 by substitution for D_i' from Relation 1. This shows the limit on D_{sb} imposed by the desired perceived image width.

The same effect as described in the preceding paragraph can be achieved by placing light baffle 32 between slitboard 22 and backboard 23, thereby obstructing 25 the view of one image 230 through the slit 220 of an adjacent image 230.

Third, one can change the shape of the backboard, as illustrated in FIG. 7. In apparatus 70, backboard 71 bears curved images 730 so that second order images are not 30 observed. The change in backboard shape will result in a slightly altered stretching effect. As before, this stretching effect can be undone by preshrinking the image in the direction of motion.

The embodiment illustrated in FIG. 7 has the potentially useful property not only of showing no second 35 order images, but also of an arbitrarily wide first order

image. This effect is related to, but distinct from, the stretching effect described above, which assumes a flat backboard geometry. The final observed width of the image is limited by the vignetting of the slitboard -- the exact
5 relation can be found by solving Relation 5 for D_i' . It can be observed from FIG. 7 that as the viewing angle becomes large, the viewer continues to observe through each given slit 220 only the image 730 corresponding to that slit 220. In the ideal limit of zero slitboard width, the
10 leftmost sliver of the image is viewable when the viewer looks 90° to the left and the rightmost sliver is viewable when the viewer looks 90° to the right. The slivers in between are continuously viewable between these extreme angles. In other words, each image is observed as
15 infinitely wide. (In FIG. 7, the curved image 730 does not quite reach the slitboard 22, in order to illustrate the maximum viewing angle allowed by the vignetting of a non-zero width slitboard. In principle, the curve of image 730 may reach the slitboard.)

20 A further relation is that the slit width must vary inversely with the light brightness -- i.e., $D_s \propto 1/B$. In general, the device has higher resolution and less blur the smaller the slit width (analogously to how a pinhole camera has higher resolution with a smaller pinhole).
25 Since smaller slits transmit less light, the brightness must increase with decreasing slit width in order that the same total amount of light reach viewer 30.

The width of slit 220 relative to the image width determines the amount of blur perceived by viewer 30 in the
30 direction of motion. More specifically, the size of slit 220, projected from viewer 30 onto backboard 23, determines the scale over which the present device does not reduce blur. This length is set because the sliver of the image that can be seen through slit 220 at any given moment is in motion, and therefore blurred in the viewer's perception. The size of slit 220 relative to the image

width should thus be as small as practicable if the highest resolution possible is desired. In the parameter ranges of the two examples below, slit widths would likely be under about 0.03125 inch (under about 0.8 mm).

- 5 The achievable brightness and resolution, and their relationship, can be quantified.

First, define the following additional parameters:

- 10 L_{ambient} = the ambient luminance of the viewer's environment
- 15 L_{device} = the luminance of the backboard on the apparatus
- 20 c = the contrast between the image and the ambient environment at the position of the viewer
- 25 $D_{\text{vb}} = D_{\text{vs}} + D_{\text{bs}}$ = the distance between the viewer and the backboard
- 30 B_{ambient} = the brightness of the ambient environment at the position of the viewer
- 35 B_{device} = the brightness of the image at the position of the viewer
- TF = the transmission fraction, or fraction of light that passes through the slitboard
- R = the image resolution
- 25 L_{ambient} describes the luminance of a typical object within the field of view of the viewer while looking at the image projected by the apparatus. This typical object should be representative of the general brightness of the viewer's environment and should characterize the background light level. For example, in a subway or train it might be the wall of the car adjacent to the window through which the apparatus is viewable.

30 B_{ambient} is the brightness of that object as seen by the viewer, and

$$B_{\text{ambient}} = L_{\text{ambient}} / 4\pi D_{\text{ambient}}^2, \quad (6)$$

- 35 where D_{ambient} is the distance between the viewer and the ambient object. It is sometimes difficult to select a

particular object as representative of the ambient. As discussed above, in an embodiment used in a subway tunnel, the ambient object could be the wall of the subway car adjacent the window, in which case D_{ambient} is the distance 5 from the viewer to the wall. For ease of calculation, this may be approximated as D_{vs} because the additional distance from the window to the apparatus is relatively small.

L_{device} describes the luminance of the images on the backboard of the apparatus. Because the backboard is 10 always viewed through the slitboard, which effectively filters the light passing through it, its brightness at the position of the viewer, B_{device} , is

$$B_{\text{device}} = (L_{\text{device}} / 4\pi D_{vb}^2) \times TF. \quad (7)$$

TF, the transmission fraction of the slitboard, is the 15 ratio of the length of slitboard transmitting light to the total length -- i.e.,

$$\begin{aligned} TF &= D_s / D_{ff} \\ &\leq (D_s \times D_{vs}) / (D_i' \times D_{bs}), \end{aligned} \quad (8)$$

where equality holds in the second line when $D_{ff} = D_i$. 20 R, the image resolution, is the ratio of the size of the image to the size of the slit projected onto the backboard,

$$\begin{aligned} R &= (D_i \times D_{vs}) / (D_s \times D_{bs}) \\ &\approx D_i / D_s \\ &= (D_i' \times D_{bs}) / (D_s \times D_{vs}) \end{aligned} \quad (9)$$

This quantity is called the resolution because the image tends to blur in the direction of motion on the scale of the width of the slit. Because the eye can see the whole area of the image contained within the slit width at the 30 same time, and the image moves in the time it is visible, the eye cannot discern detail in the image much finer than the projected slit width. Therefore D_s effectively defines the pixel size of the image in the direction of motion. In other words, for example, if the slit width is one-tenth 35 the width of the image, the image effectively has ten pixels in the direction of motion. In practice, the eye

resolves the image to slightly better than R, but R determines the scale.

In order that the image meaningfully project a non-blurry image, R preferably is greater than 10, but this may depend on the image to be projected. It should also be noted that $R = 1/TF$ when $D_i = D_{ff}$, so that increasing the resolution decreases the transmitted light.

c is the contrast between the apparatus image and the ambient environment at the position of the viewer. In order that the image be viewable in the environment of the viewer, the apparatus brightness must be above a minimum brightness

$$B_{device} \geq B_{ambient} \times c. \quad (10)$$

In order that the device be visible at all, c defines a minimum device brightness that depends on the properties of the human eye: if the device's image is too dim relative to its environment it will be invisible. The brightness of the device may always be brighter than the minimum defined by c. Practically speaking, c ought to be at least about 0.1. For many applications, such as commercial advertising, it may be desirable that c be greater than 1.

The following parameters comprise the smallest set of parameters (which may be referred to as "independent" parameters) that fully describe the apparatus according to the invention -- D_{vs} , D_{bs} , V_w , $L_{ambient}$, $D_{ambient}$, c, L_{device} , D_i , D_s , and D_{ff} . Other parameters, which may be defined as "dependent parameters" are:

$$D_i' = D_i \times D_{vs}/D_{bs}$$

$$D_{vb} = D_{vs} + D_{bs}$$

$$R = D_i/D_s$$

$$FR = V_w/D_{ff}$$

$$TF = D_s/D_{ff}$$

$$B_{ambient} = L_{ambient}/4\pi D_{ambient}^2$$

$$B_{device} = (L_{device}/4\pi D_{vb}^2) \times TF$$

Of the independent parameters, the first five are substantially determined by the environment in which the

apparatus is installed. In a subway system, for example, these five parameters are determined by the cross sections of the tunnel and train, the train speed, and the lighting in the train. On a pedestrian walkway or building
5 interior, as another example, these parameters are determined by the dimensions of the walkway or hallway, pedestrian foot speed, and the ambient lighting conditions.

c and the dependent parameters R and FR are constrained by properties of human perception, and that the
10 image of the apparatus be meaningful and not overly degraded by blurring. D_i' is constrained either by the environment (the width of a subway window, for example) or by the requirements of the image to be displayed by the apparatus (such as aesthetic considerations) or both. The
15 remaining dependent parameters are determined by the independent parameters.

When these parameters are not substantially constrained, much greater leeway is allowed with the remaining four independent parameters, and the specific
20 relationships set forth below need not be followed. Such relaxed conditions occur, for example, in connection with a surface train traveling outdoors in a flat environment when D_{vs} is largely unconstrained. Sometimes a substantially unconstrained parameter results in an environment where the
25 apparatus cannot be used at all, such as where the ambient light level varies greatly and randomly or the viewer speed is completely unknown.

The constraints on the remaining independent parameters are best expressed as a series of inequalities
30 and are derived below.

Combining Relations 6, 7 and 10 provides the minimum slit width,

$$\begin{aligned} D_s &\geq c \times (B_{\text{ambient}}/B_{\text{device}}) (D_{bs} \times D_i') / D_{vs} \\ &\geq c \times (L_{\text{ambient}}/L_{\text{device}}) (D_{vb}^2/D_{\text{ambient}}^2) (D_{bs} \times D_i') / D_{vs} \end{aligned} \quad (11)$$

35 Solving Relation 9 for D_s gives,

$$D_s \leq (D_i' \times D_{bs}) / (R \times D_{vs}). \quad (12)$$

Combining Relations 11 and 12 constrains the slit width from above and below:

$$c \times (L_{ambient}/L_{device}) (D_{vb}^2/D_{ambient}^2) (D_{bs} \times D_i') / D_{vs} \leq D_s \leq (D_i' \times D_{bs}) / (R \times D_{vs}) \quad (13)$$

- 5 In this relation, $L_{ambient}$ and all the distances except the slit width are substantially constrained by the environment, and R and c are constrained by properties of human visual perception. As discussed above, for ease of calculation, $D_{ambient}$ can be approximated by D_{vs} ; note also
10 that $(D_{bs} \times D_i') / D_{vs} = D_i$. The inequality between the far left and far right sides of the relation forces a minimum luminance for the apparatus, L_{device} . That is, if the luminance of the apparatus is below a minimum threshold, the apparatus image will be too dim to see in the
15 brightness of the viewer's environment.

Once the luminance of the apparatus is sufficiently high, the inequalities between D_s and the far left and far right of the relation determine the allowable slit width range. A smaller slit width gives higher
20 resolution but less brightness and a greater slit width gives brightness at the expense of resolution. A higher luminance of the apparatus extends the lower end of the allowable slit width range.

Another similar relation for the frame-to-frame spacing may be derived from the relations above.

Relation 3 may be written

$$\begin{aligned} D_{ff} &\geq D_i \\ &\geq (D_i' \times D_{bs}) / D_{vs}. \end{aligned} \quad (14)$$

Relation 2, frame rate = V_w/D_{ff} , may be rewritten

$$30 \quad D_{ff} \leq V_w/FR, \quad (15)$$

where FR denotes the frame rate and the equality has changed to an inequality to reflect that FR is a minimum frame rate necessary for the animation effect to work.

Combining Relations 14 and 15 yields,

$$(D_1' \times D_{bs})/D_{vs} \leq D_{ff} \leq V_w/FR. \quad (16)$$

V_w and all the distances except D_{ff} are substantially constrained by the environment, and FR is constrained by properties of human visual perception. Therefore the
5 relation defines an allowable range for D_{ff}. It also puts a condition on the environments in which the present invention may be applied -- i.e., if the inequality does not hold between the far left and far right hand sides of the relation, the present invention will not be useful.

10 Choosing a lower D_{ff} puts second order frames closer to first order frames while improving the frame rate. Decreasing D_{ff} also increases the transmission fraction without decreasing the resolution. Choosing a higher D_{ff} moves the images farther apart at the expense of
15 a reduced frame rate.

Though in principle apparatus 10 requires no included light source for its operation if ambient light is sufficient, such as outdoors (lid 21 or backboard 23 would have to be light-transmissive), in practice the use of very
20 thin slits does impose such a requirement. That is, when operated under conditions of low ambient light and desiring moderate resolution, bright interior illumination is preferable. The designation "interior" indicates the volume of the apparatus 10 between backboard 23 and
25 slitboard 22, as opposed to the "exterior," which is every place else. The interior contains the viewable images 230, but otherwise may be empty or contain support structure, illumination sources, optical baffles, etc. as described above in connection with FIGS. 1, 2 and 2A.

30 Moreover, this illumination preferably should not illuminate the exterior of the device, or illuminate the viewer's environment or reach the viewer directly, because greater contrast between the dark exterior and bright interior improves the appearance of the final image. This
35 lighting requirement is less cumbersome than that for stroboscopic devices -- in a subway tunnel environment,

this illumination need not be brighter than achievable with ordinary residential/commercial type lighting, such as fluorescent tubes. The lighting preferably should be constant, so no timing complications arise. Preferably the 5 interior of apparatus 10 should be physically sealed as well as possible from the exterior subway tunnel environment as discussed above, preferably while permitting dissipation of heat from the light source, if necessary. The enclosure may also be used to aid the illumination of 10 the interior by reflecting light which would otherwise not be directed towards viewable images 230.

Two examples show in more detail how the various parameters interrelate.

Example 1

15 The first example illustrates how all constraints tend to relax as V_w increases. For example, in a typical subway system the following parameters may be imposed:

$$V_w \approx 30 \text{ mph} \quad (\text{train speed})$$

$$D_{bs} \approx 6 \text{ inches} \quad (\text{space between train and wall})$$

20 $D_{vs} \approx 6 \text{ feet}$ (half the width of a train, for the average location of a viewer 30 within the car)

$$D_i' \approx 3 \text{ feet} \quad (\text{width of train window})$$

By Relations 3 and 1,

$$\begin{aligned} D_{ff} &\geq D_i \\ &\geq (D_i' \times D_{bs}) / D_{vs} \\ &\geq (3 \text{ ft} \times 0.5 \text{ ft}) / 6 \text{ ft} \\ &\geq 0.25 \text{ feet.} \end{aligned} \tag{17}$$

If the images are abutted so that $D_{ff} = D_i$, the maximum 30 frame rate is attained. Then, by Relation 2,

$$\begin{aligned} \text{Frame rate} &= 30 \text{ mph} / 0.25 \text{ ft} \\ &= 176 \text{ frames per second.} \end{aligned} \tag{18}$$

At this rate the parameters can be adjusted a great deal while still maintaining high quality animation. This frame 35 rate is also high enough to support interlacing of images

(see above) if desired, despite the reduction in effective frame rate that results from interlacing.

Example 2

The second example illustrates how the
5 constraints tighten when near the minimal frame rate. To find the lowest practicable V_w , assume the following parameters:

$$\begin{aligned} \text{frame rate} &\approx 20 \text{ frames/sec} \\ D_{bs} &\approx 6 \text{ inch} \\ 10 D_{vs} &\approx 6 \text{ feet} \\ D_i' &\approx 2 \text{ feet.} \end{aligned}$$

By Relation 1,

$$\begin{aligned} D_i &= (D_{bs} \times D_i') / D_{vs} \\ &= (0.5 \text{ ft} \times 2 \text{ ft}) / 6 \text{ ft} \\ 15 &= 2 \text{ inches.} \end{aligned}$$

For abutted images, $D_{ff} = D_i$, and,

$$\begin{aligned} V_w &= D_{ff} \times \text{frame rate} \\ &= 2 \text{ inches} \times 20 \text{ frames/sec} \\ &= 40 \text{ inches/sec,} \end{aligned}$$

20 which is approximately pedestrian footspeed.

The implication of this last result -- that the device can successfully display quality animations to pedestrian traffic -- vastly increases the potential applicability of this device relative to stroboscopically 25 based arrangements.

The following alternative exemplary embodiments are within the spirit and scope of the invention.

FIG. 8 illustrates another exemplary embodiment 80 altering the optimal viewing angle of the 30 animation. In apparatus 80, backboard 83 bears images 830 that are inclined at an acute angle to backboard 83, varying the viewing angle from a right angle to that acute angle. This alteration permits more natural viewing for a pedestrian, for example, by not requiring turning of the

pedestrian's head far away from the direction of motion. This embodiment may also eliminate second order images.

FIG. 9 illustrates a further exemplary embodiment 90 similar to apparatus 80, but in which 5 slitboard 92 is also angled. This refinement again provides a more natural viewing position for a pedestrian. The asymmetric triangular design permits natural viewing for viewers moving from left to right. A symmetric design (not shown), in which the plan of the slitboard might more 10 resemble, for example, a series of isosceles triangles, could accommodate viewers moving in both directions.

FIG. 10 illustrates a technique of using one slitboard 101 as the backboard of a different slitboard 102, while simultaneously using that 15 slitboard 102 as the backboard of the original slitboard 101. This configuration permits the back-to-back installation of two devices in the space of one. This apparatus 100 may be improved by offsetting one set of slits from the other by $D_i/2$, or some fraction of D_i .

20 FIG. 11 shows a simple schematic plan view of apparatus 100. Slits 220 of one slitboard 101 are centered between slits 220 of the opposite slitboard 102, which is acting as the former slitboard's backboard. That is, between slits 220 of one slitboard are images 230 viewable 25 through the other slitboard, and vice-versa. Because the slits are very thin, their presence in the backboard creates negligible distraction.

FIG. 12 shows another embodiment 120 similar to apparatus 100, but having a set of curved images 1230 (as 30 in FIG. 7) facing slits 220 of opposite slitboards/backboards 101, 102. Apparatus 120 thus has characteristics, and advantages, of both apparatus 70 and apparatus 100.

35 FIG. 13 illustrates a roller type of image display mechanism 130 that may be placed at the position of the backboard. The rollers may contain a plurality of sets

of images that can be changed by simply rolling from one set of images to another. Such a mechanism allows the changing of images to be greatly simplified. In order to change from one animation to another, instead of manually 5 changing each image, one may roll such rollers to a different set of images. This change could be performed manually or automatically, for instance by a timer. By incorporating slits 220, mechanism 130 can be used in apparatus 100 or apparatus 120.

10 Yet another exemplary embodiment 140 is shown in FIGS. 14 and 15. In apparatus 140, "backboard" 141, with its images 142, is placed between viewer 30 and a series of mirrors 143. Each mirror 143 preferably is substantially the same size and orientation as any slits that would have 15 been used in the aforementioned embodiments. Mirrors 143 preferably are mounted on a board 144 that takes the place of the slitboard, but mirrors 143 could be mounted individually or on any other suitable mounting. The principles of operation of apparatus 140 are substantially 20 the same as those for the aforementioned embodiments. However, because "backboard" 141 would obscure the sight of mirrors 143 by viewer 30, "backboard" 141 may be placed above or below the line of sight of viewer 30. As shown in FIGS. 14 and 15, "backboard" 141 is above the line of sight 25 of viewer 30. As drawn in FIGS. 14 and 15, moreover, both "backboard" 141 and "mirrorboard" 144 are inclined. However, with proper placement, inclination of boards 141, 144 may not be necessary. As in the case of a slitboard, "mirrorboard" 144 will work best when its non-mirror 30 portions are dark, to increase the contrast with the images.

A complete animation displayed using the apparatus of the present invention for use in a subway system may be a sizable fraction of a mile (or more) in length. In accordance with another aspect of the 35 invention, such an animation can be implemented by breaking

the backboard carrying the images for such an animation into smaller units, providing multiple apparatus according to the invention to match the local design of the subway tunnel structure where feasible. Many subway systems have
5 repeating support structure along the length of a tunnel to which such modular devices may be attached in a mechanically simplified way.

As an example, the New York City subway system has throughout its tunnel network regularly spaced columns
10 of support I-beams between many pairs of tracks.

Installation of apparatus according to the present invention may be greatly facilitated by taking advantage of these I-beams, their regular spacing, and the certainty of their placement just alongside, but out of, the path of the
15 trains. However, this single example should not be construed as restricting the applicability to just one subway system.

The modularization technique has many other advantages. It has the potential to facilitate
20 construction and maintenance, by taking advantage of structures explicitly designed with the engineering of the subway tunnels in mind. The I-beam structure is sturdy and guaranteed not to encroach on track space. The constant size of the I-beams consistently regulates D_{bs} , easing
25 design considerations: Additionally, cost and engineering difficulties are reduced insofar as the apparatus may be easily attached to the exterior of the supports without drilling or possibly destructive alterations to existing structure.

30 FIG. 16 schematically illustrates an example of the modularization possible for the two-sided apparatus of FIGS. 10 and 11. As shown, construction of the whole length of two slitboards, which could be a half mile or more in length, is reduced to constructing many identical
35 slitboards 160, each about as long as the distance between adjacent I-beam columns 161 (e.g., about five feet). Each

of the slitboards is then attached to a pair of the existing support I-beams, along with the other parts of the apparatus as described above.

FIG. 17 schematically illustrates the side profile of display apparatus 1700, which includes slitboard 1722 and backboard 1723. Slitboard 1722 and backboard 1723 are parallel to each other, planar, and perpendicular to a viewer's line of sight 1701. Also shown are viewer-to-backboard distance, D_{vb} , and backboard-to-slitboard distance, D_{bs} . As described above, D_{vb} and D_{bs} are well defined for any viewer's horizontal line of sight and, accordingly, so is the magnification factor. For a non-horizontal line of sight, D_{vb} and D_{bs} both increase by a factor of $1/\cos \theta$ (where θ is measured from the horizontal), so the magnification factor remains the same. This cancellation allows display apparatus with a vertical slitboard and a vertical backboard to project images whose magnification is constant in the vertical direction.

FIG. 18 shows a subway tunnel 1802 in which display apparatus 1700 is mounted on each side of the tunnel wall. Walkway 1804 and subway car 1806, with windows 1808, are also shown. Walkway 1804 is an access catwalk used by maintenance personnel and is typically only wide enough for one person (walkway 1804 is not a subway station platform used by subway passengers). Because subway tunnels are built to accommodate subway trains and not necessarily display apparatus, some subway tunnels have very limited space for installation of such display apparatus. Thus, for example, display apparatuses 1700 leave little clearance for either subway car 1806 or a person on walkway 1804, as shown in FIG. 18. Therefore, a less spatially protrusive display apparatus would improve the safety of passing trains 1806 and maintenance personnel on walkway 1804. Moreover, such apparatus would likely be easier to install and maintain.

Advantageously, an embodiment of a slanted display apparatus 1900 constructed in accordance with the invention is provided. Display apparatus 1900 is shown in FIG. 19 mounted in subway tunnel 1802. Both slitboard 1922 and backboard 1923 are slanted outward to conform better to the available space in tunnel 1802. Display apparatus 1900 accordingly provides increased clearance, and thus safety, for both subway car 1806 and persons walking on walkway 1804.

In accordance with the invention, determination of the various display apparatus parameters discussed above are advantageously the same for apparatus 1900 as they are, for example, for display apparatus 1700, which has a slitboard and backboard perpendicular to a viewer's horizontal line of sight. The determination is the same because the magnification effect of slanted display apparatus 1900 is also constant in the vertical direction provided both the slitboard and backboard are slanted by the same angle. In other words, the magnification factor is constant with respect to viewing angle.

Referring to FIGS. 20 and 21, this constant magnification effect can be shown via similar triangles. Note that line segment BD is parallel and equal in length to line segment CF. Thus,

$$\frac{AE}{AD} = \frac{CE}{CF} = \frac{CE}{BD} \quad (19)$$

or

$$\frac{AE}{CE} = \frac{AD}{BD} \quad (20)$$

Substituting display apparatus parameters in accordance with the invention yields:

$$\frac{D_{vb}'}{D_{bs}'} = \frac{D_{vb}}{D_{bs}} \quad (21)$$

Thus, the magnification factor is constant with respect to viewing angle θ .

Note that to obtain substantially the same space-saving advantage of display apparatus 1900, display 5 apparatus 1700 can be advantageously installed by simply tilting apparatus 1700 inward.

FIG. 22 shows an embodiment of a curved display apparatus 2200 constructed in accordance with the invention mounted in subway tunnel 1802. Both slitboard 2222 and 10 backboard 2223 are curved outward to conform even better than display apparatus 1900 to the available space in tunnel 1802. This embodiment, therefore, provides even more clearance and safety than apparatus 1900.

Advantageously, display apparatus constructed in 15 accordance with the invention can include some arbitrary slitboard and backboard geometries that enable it to conform to a wide range of available spaces. Examples of such arbitrary geometries are shown in FIGS. 23 and 24.

FIG. 23 shows an embodiment of nonplanar display 20 apparatus 2300 in accordance with the invention.

Apparatus 2300 includes nonplanar slitboard 2322 and nonplanar backboard 2323, which are non-vertical and have the same profile (i.e., they are parallel). FIG. 24 shows another embodiment of nonplanar display apparatus 2400 in 25 accordance with the present invention. Apparatus 2400 includes nonplanar slitboard 2422 and nonplanar backboard 2423, which are non-vertical and do not have the same profile (i.e., they are not parallel). Neither slitboard 2322 and backboard 2323 nor slitboard 2422 and 30 backboard 2423 are perpendicular to a viewer's respective lines of sight 2301 and 2401. Note that the slitboard and backboard profiles shown in FIGS. 23 and 24 are merely illustrative and should in no way limit the invention.

Further note that because of the magnification 35 effect, not all slitboard and backboard geometries result

in acceptable animation. In theory, display apparatus that provides a constant magnification for more than one viewer position (e.g., the optimal position) is possible for only a few geometries. Viewers at other positions will observe
5 images whose magnification varies up and down the backboard, resulting in a warped looking image -- overly magnified at some positions and under-magnified at others. In practice, however, the amount of warping is often within acceptable limits for viewing positions close to the
10 optimal viewing position.

An obstacle to designing display apparatus having arbitrary slitboard and backboard geometries is finding the magnification factor, which varies with position along the backboard. The magnification factor depends on viewer
15 position, which determines both D_{vb} and D_{bs} . Once a viewer position, designated by coordinates (x_v, y_v) , is chosen, magnification factor, m , can be found for each position on the backboard, designated by coordinates (x_b, y_b) . That is,
20 m is a function of x_v , y_v , x_b , and y_b . Preferably, images of a display apparatus are visible from a range of viewer positions.

Note that the following assumes that the display apparatus is substantially parallel to the viewer's direction of motion (which for FIGS. 19-24 is into and out
25 of the page, or in the z direction). Thus, reference to a viewer's position, or position along a slitboard or backboard, refers to position in the cross-sectional or side-elevational plane (e.g., with respect to FIGS. 23 and 24, the x-direction is horizontal and the y-direction
30 is vertical).

FIG. 25 is a flow diagram of an exemplary process 2500 for determining whether a display apparatus with arbitrary slitboard and backboard geometries results in acceptable animation in accordance with the invention.
35 At 2502, side profiles of a slitboard and a backboard (as shown, for example, in FIGS 23 and 24) are selected. This

selection is preferably in accordance with available installation space. These profiles are preferably smooth with no jumps or sharp corners. Preferably, they monotonically rise, meaning that any horizontal line 5 crossing the profile crosses it at most one point. Should the profiles not meet these preferences, appropriate modifications to process 2500 may be necessary, although much of the process will remain unchanged.

At 2504, each board profile is represented by a 10 mathematical function (e.g., $f_{backboard(x,y)}$ and $f_{slitboard(x,y)}$), which can be an approximation.

At 2506, an optimal viewer position $(x_{v,OPT}, Y_{v,OPT})$ is selected. This selection should be made in accordance with the available installation space and most likely or 15 average position of a viewer. For example, in a subway tunnel, this position might be in the center of a subway car at the average height of a person. On a pedestrian walkway, this position might be in the middle of the walkway also at the average height of a person.

At 2508, a worst case viewer position (x_w, y_w) is selected in order to determine whether the chosen profiles will yield acceptable images for viewers away from the optimal position. For example, a worst case position for the subway tunnel installation may be at the seat closest 25 to the window. The worst case position should be the one that results in the most warped observed image. Typically, a worst case position is the farthest from $(x_{v,OPT}, Y_{v,OPT})$, but not necessarily.

At 2510, a worst case magnification delta or 30 limit, ML, is selected. Limit ML represents the largest acceptable difference between magnification as observed from the optimal position and magnification as observed from the worst case position. For example, an ML of $\pm 10\%$ may be set as the largest acceptable magnification 35 difference between the two magnifications (i.e., the difference between the worst case position magnification

and the optimal position magnification should be no more than $\pm 10\%$. The selection of ML can be arbitrary and can depend on the degree of tolerable image warpage for a particular display apparatus application.

5 The magnification factor is preferably determined as a function of position along the height of the backboard (i.e., the y-direction as defined above). Assuming the preferences above, the position on the backboard is referred to as y_b , which can vary from the bottom of the
10 backboard, $y_{b,low}$, to the top of the backboard, $y_{b,hi}$, and for which each y_b , there is a unique x_b .

The optimal viewer's line of sight, $f_{LOS}(x,y)$, -- that is, the line joining $(x_{v,opt}, Y_{v,opt})$ and (x_b, y_b) -- is now uniquely determined at 2512. The point where the viewer's
15 line of sight to the backboard crosses the slitboard, (x_s, y_s) , is the intersection of the two equations for f_{LOS} and $f_{SLITBOARD}$.

The magnification for a viewer's position as a function of (x_b, y_b) can be determined as follows once the
20 viewer-to-backboard and backboard-to-slitboard distances are known:

$$D_{vb} = \sqrt{(x_b - x_{v,opt})^2 + (y_b - Y_{v,opt})^2} \quad (22)$$

$$25 \quad D_{bs} = \sqrt{(x_b - x_s)^2 + (y_b - y_s)^2} \quad (23)$$

$$m_{opt}(x_{v,opt}, Y_{v,opt}, x_b, y_b) = D_{vb} / D_{bs} \quad (24)$$

Because $x_{v,opt}$ and $Y_{v,opt}$ are fixed and x_b is determined by y_b , the magnification can be referred to as $m_{opt}(y_b)$ without confusion.

30 At 2514, the same procedure is followed for determining the magnification factor, m_w , for the worst viewer position.

At 2516, $m_{opt}(y_b)$ and $m_w(y_b)$ are compared in view of limit ML. If the difference between the two

magnifications is less than or equal to ML, as calculated below:

5
$$\left| \frac{m_{opt}(Y_b) - m_w(Y_b)}{m_{opt}(Y_b)} \right| \leq ML \quad (25)$$

the selected profiles for the slitboard and backboard will result in acceptable observed images. Process 2500 then moves to 2518, where images are preshrunk as described above in accordance with $m_{opt}(Y_b)$.

10 If the difference between the two magnifications is greater than ML, indicating unacceptable observed images, process 2500 returns to 2502 where the process repeats with new selected profiles for the slitboard and backboard.

15 Note that process 2500 can also be used to design display apparatus having curved slitboard and backboard profiles such as display apparatus 2200.

20 Thus it is seen that display apparatus for use in spatially-constrained environments is provided that displays still images that appear animated to viewers in motion relative to the apparatus. One skilled in the art will appreciate that the present invention can be practiced by other than the described embodiments, which are presented for purposes of illustration and not of
25 limitation, and the present invention is limited only by the claims which follow.